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Principles of Physics in Physiology

Several areas of physiology cannot be appreciated without an elementary knowledge of physics. If only to emphasize the point, selected principles of physics that are important in physiology are outlined below. Also discussed are mathematical principles that are inseparable from physics.

Mathematics

Vectors

Vectors are quantities that have a *magnitude* as well as a *direction*. A vector is represented with an arrow that indicates its direction. The length of the arrow gives a measure of the magnitude of the vector. A vector can be resolved into *components*. Conversely, two or more vectors can be combined into a *resultant* vector. Physiological applications of vectors are found in biomechanics, electrocardiography, motor control, and vestibular mechanisms, among others. The basic concepts of vector resolution are explained with the following examples.

Suppose a person travels 150 km from point O to point P (Fig. 1.1A). In doing so, he travels 138 km to the south, 60 km to the east, and 140 km to the southeast. The distance he travels in a given direction can be calculated simply by dropping a perpendicular from point P onto the axis representing that direction. This basic method can be applied to any vector quantity. For example, if the person travels from point O toward point P with a velocity of 150 km/h, then he moves south with a velocity of 138 km/h, toward east with a velocity of 60 km/h, and toward southeast with a velocity of 140 km/h. Conversely, if it is known at what velocity he is moving toward south and east, the actual velocity and direction of his movement can be calculated graphically.

A vector does not have any component perpendicular to it. This is self-evident; a person traveling due south does not move toward east or west. The calculation of the *mean electrical axis of the heart* from the recorded voltages in the electrocardiogram (ECG) leads (see **Fig. 34.11**) is based on the same principle. It explains why an ECG wave that has the highest amplitude in lead I would have the lowest amplitude in lead augmented vector foot (aVF) which is perpendicular to lead I. Vector principles also explain why the *effect of gravity on* **blood circulation** gets nullified when the body is supine. In the supine position, the direction of gravity is perpendicular to the direction of blood flow in most of the large vessels.

A special case of the vector principle is illustrated in **Fig. 1.1B**. Suppose a person is standing at point O situated at the center of an equilateral triangle formed by points A, B, and C. When the person moves toward point P with a velocity of (say) 70 km/h, he is moving toward point A at 51 km/h, toward point B at 16 km/h, and toward point C at -67 km/h. (The minus sign denotes that he is actually moving away from point C.) On adding the three velocities, we get zero. This principle forms the basis of the zero potential obtained by interconnecting the vertices of *Einthoven triangle of electrocardiography*.



Fig. 1.1 Vector principles. [A] Resolution of a vector into its components. [B] Vector principles underlying Einthoven hypothesis of electrocardiography.

Calculus

There are two broad branches of calculus: differential and integral. Both find applications in several areas of physiology.

Differential calculus makes it possible to calculate the slope of a curve at any point. The slope of a line segment is expressed mathematically as $\delta y/\delta x$, where δy is the small vertical distance through which a point on the segment moves up as it shifts a small distance δx to the right. In the case of a straight line, this ratio remains the same anywhere along the line but in the case of a curved line, this ratio is different for every small segment of the line (Fig. 1.2A). Clearly, a precise description of the slopes of various parts of a curve requires that we break up the curve into infinitesimally small segments. The slope of each segment, which is small enough to be called a *point*, is denoted by the expression *dy/dx*.

Integral calculus makes it possible to calculate the *area under the curve* in a Cartesian plane. The area under the curve can be calculated by breaking up the area into rectangular blocks. However, if the curve is irregular, the blocks are not perfect rectangles and the result obtained is inaccurate. Greater accuracy is possible only if the width of blocks is infinitesimally small (dx) so that each block becomes a perfect rectangle. The area under the curve (A) is then given by:

Or stated simply, A is the sum of areas of an infinite number of rectangles with an infinitesimally small width (dx) so that the area of each rectangle is given by $y \times dx$. It should be readily apparent from **Fig. 1.2B** that $\int y dx$ is *not the same* as $\int x dy$.

The graphic calculation of the *work done* by the lung and heart, the *pressure-time index* of the heart and *mean blood pressure*, and the amount of dye flowing in the *indicator dilution method* of blood flow estimation are based on the principles of integral calculus.

Logarithms

The logarithm of a number is the exponent to which 10 must be raised so as to equal the number. Expressed mathematically, if $10^a = N$, then log N = a. For example, log 1,000 = 3 and log 0.001 = -3. It may be noted here that 1,000 and 0.001 are reciprocal numbers. In other words, if *log N* = *a*, then *log 1/N* = -*a*. Logarithms appear in the *Nernst equation* (p 19). In accordance with the logarithmic property



Fig. 1.2 [A] (*Left*) The slope $(\delta y/\delta x)$ is the same in all segments of a straight line. (*Right*) For the same δx , the δy varies in different segments of the curve. Hence the slope $(\delta y/\delta x)$ is different in all segments. [B] Areas defined by the terms [Xdy (*left*) and [Ydx (*right*).

just explained, the Nernst equation can be written in either way as follows:

or

 $Em = \frac{61}{z} \log \frac{[C_o]}{[C_i]}$ $Em = \frac{-61}{z} \log \frac{[C_i]}{[C_i]}$

An important application of logarithms is the *logarithmic scale* which is a convenient scale for describing certain types of data. Consider the sound pressure from various sources (**Table 1.1**). The inadequacy of a linear scale in representing these data graphically is obvious from **Fig. 1.3**. On the other hand, if the data are converted into their logarithms and then plotted, the advantage is instantly apparent. The logarithmic scale of *sound intensity* is called the *decibel scale*. Similarly, the logarithmic scale of *acidity* is the *pH scale*.

 Table 1.1 Sound pressures at auditory threshold and in different situations

	Sound pressure in dyne/ cm ²	Sound pressure as a mul- tiple of threshold	Log of the multiple
Threshold	0.002	1	0
Conversation	0.02	10	1
Factory noise	2	1,000	3
Discomfort	200	100,000	5



Fig. 1.3 Sound pressures expressed as multiples of hearing threshold are depicted graphically on a linear scale (*above*) and a logarithmic scale (*below*).

Mechanics

Laws of motion

The *first law of motion* states that a body continues to be stationary or to move in a straight line with uniform velocity until it is acted upon by an external force. The law helps in defining force itself (see below). The law is also known as the *law of inertia*. Because of inertia, a stationary body cannot start moving on its own and a moving body cannot stop on its own. The concept of inertia helps in understanding the effect of *coup and counter-coup injuries* of the brain and the working of the *semicircular canals* of the vestibular apparatus.

The **second law of motion** tells us that the acceleration or retardation of a body is directly proportional to the force applied on it and inversely proportional to the mass of the body. The product of the mass and acceleration of a body gives the force acting on it.

The *third law of motion* states that every action has an equal and opposite reaction. The third law has been put to use in *ballistocardiography*. It also helps in understanding *muscle action* (see **Fig. 49.3**).

Force

Force is anything that changes or tends to change the uniform motion of a body in straight line. The SI



Fig. 1.4 Shearing force.

unit of force is the Newton (N). A force of 1 N, when applied to a 1 kg mass placed on a horizontal frictionless surface, produces an acceleration of 1 m/s².

A *shearing force* is a force that is directed tangentially to the surface of a body (**Fig. 1.4**). Under the effect of a shearing force, the constituent laminae of a body move through different distances. An understanding of the nature of shearing force is important in the context of *otolith organs*. Shearing force is also *exerted by blood flow on the capillary endothelium*.

Gravitational force, as applicable on earth, is a special kind of force that has two remarkable features: (1) it is *always directed toward the center of the earth* and, thereby, defines the vertical. (2) It is *directly proportional to the mass of the body*. The acceleration produced by gravitational force is called *acceleration due to gravity*. A heavier body is pulled with a greater gravitational force (in accordance with Newton law of gravitation). However, for a given force, a heavier body has less acceleration (in accordance with Newton second law of motion). Therefore the acceleration due to gravity does not vary with the mass of a body and remains absolutely constant at 9.8 m/s². This acceleration due to gravity, denoted by g, gives us *the feel of weight*.

G forces are accelerative forces other than gravity that may act on the body in specific situations. The accelerative force is called **G***x* when it is directed anteroposteriorly, **G***y* when it is directed laterally, and **G***z* when it is directed superoinferiorly in reference to the body. Together, the Gx, Gy, and Gz forces are called **G** forces.¹ The organs for sensing G forces are the otolith organs.

The weight felt by a subject under the effect of Gz is called the *apparent g*. Changes in Gz have important effects on cardiac output, blood pressure, and

¹G conventionally denotes the universal gravitational constant. In certain special contexts, as in aerospace medicine, G denotes a variable whose value is expressed in multiples of g, for example, 2, –1, or 0 g. The term G-force is a misnomer because a change in G-force is almost always due to acceleratory forces other than gravitational force.

pulmonary ventilation that are described on p 257. *High and low Gz* are experienced when there is acceleration or deceleration along the long axis of the body. Very high Gz occurs *when a space rocket takes off.* More commonly, such changes in Gz are experienced during *looping of airplanes* and during *parachute jumping* when the parachute is suddenly opened out after a period of free fall: It is called the **opening shock** load. A slight feel of high and low Gz is *experienced in an elevator when it starts or stops.*

Zero Gz is perceived by astronauts in orbiting satellites where the gravitational force is precisely counterbalanced by the centrifugal force generated by the orbiting satellite. On earth, zero Gz is experienced during free fall under the effect of gravity. Stated mathematically

where

Gz = apparent acceleration due to gravity a = actual acceleration in the direction of gravity g = 9.8 m/s²

When a = g, Gz becomes 0. In other words, a body falling under the effect of gravity is weightless (see **Fig. 38.15**).

Pressure

Pressure is the *force exerted per unit area*. The pressure of a column of fluid is called *hydro-static pressure*. It depends only on its *verti-cal height*; neither the width of the column nor its inclination makes any difference to the pressure exerted (**Fig. 1.5A**). This concept is of importance in understanding the measurement of *jugular venous pressure* and the *direct manometry* of blood pressure. The dependence of fluid pressure on the height of the fluid column also explains why the *venous pressure is higher in the dependent parts of the body* and why the *atmospheric pressure decreases at high altitudes*. Its knowledge helps in estimating the *pressure at different depths* of the sea, which is important in deep-sea diving.

The *SI unit of pressure* is N/m^2 , which is also called *Pascal* (Pa). The atmospheric pressure at sea level is taken as 101.29 kilopascals (kPa). This pressure is also known as *1 atmosphere absolute* (*ATA*). The value of 1 atmospheric pressure, when rounded off to 100 kPa, is called *1 bar*. However, fluid pressure is often expressed simply in terms of the *vertical height of a fluid column* because the pressure of a fluid column is given by $h\rho g$ where "h" is the height of the fluid column and " ρ " is the density of the fluid. The fluid of reference is usually



Fig. 1.5 [A] Hydrostatic pressure depends only on the vertical height of a fluid column. It remains unaffected by the diameter and inclination of the tube. [B] A mercury manometer connected to a rubber cuff is used in sphygmomanometry. (*Above*) The cuff pressure is zero and the mercury levels in the reservoir and manometer tube are equal. (*Below*) As the cuff pressure increases, the mercury level in the tube rises while the mercury level gives the cuff pressure. Due to the fall in mercury level in the reservoir, the fixed scale gives a false-high reading due to positive zero error. The error can be reduced somewhat by scaling down the calibration. It can be verified that in a sphygmomanometer, the 1 cm calibration is actually a little less than 1 cm.

mercury but can be water, saline, or even blood, whichever is convenient. The pressure exerted by *1 mm of mercury column* is called *1 Torr*. Nearly all fluid pressures inside the body are a few millimeters of mercury above or below the atmospheric pressure, which makes the Torr a convenient unit for expressing physiological pressures. Since mercury is 13.6 times denser than water, 1 Torr equals *13.6 mm of water pressure*.

Even atmospheric pressure is commonly expressed in terms of the height of the mercury column that would counterbalance it. The height can be calculated, given that the density of mercury is $13.6 \times 10^3 \text{ kg/m}^{-3}$:

Atmospheric pressure $= h \times \rho \times g$ $101.29 \times 10^3 = h \times (13.6 \times 10^3) \times 9.8$ $\therefore \qquad h = 0.76 \text{ m}$ = 760 mm

Hence, atmospheric pressure is also expressed as 760 mm of mercury, or 760 Torr.

The *mercury manometer* (Fig. 1.5B) is commonly used for measuring pressure. One limb of the manometer is connected to the system whose pressure is to be measured. The other limb of the manometer is left open to the atmosphere. The difference in the mercury column in the two limbs indicates *the pressure of the system in excess of the atmospheric pressure*.

Levers

A lever is a rigid bar that is acted on by forces that tend to rotate the bar about its pivot or fulcrum. Levers are of three types depending on the relationship between the fulcrum, load (weight), and effort (force) applied. If the fulcrum (F) is central, it is a *class-I lever*. If the load (L) is central, it is a *class-II lever*. If the effort (E) is central, it is called a *class-II lever*.

The *mechanical advantage* of a lever is the *ratio of the load force to the effort force*. The ratio is proportional to the ratio of effort arm to load arm (**Fig. 1.6**). The greater the mechanical advantage, the less will be the force required to move a load.

Mechanical advantage =
$$\frac{\text{Load}}{\text{Effort}}$$

The **velocity ratio** is the ratio of the distance moved by the effort to that moved by the load. The greater the velocity ratio, the greater is the distance through which an effort has to move for lifting a load.

$$Velocity ratio = \frac{Distance moved by effort}{Distance moved by load}$$

In a frictionless lever, *mechanical advantage* equals velocity ratio. Therefore, in all three classes, what is gained in excursion of the load is lost in the effective force acting on the load and vice versa. *Class-II levers* always produce force gains, and *class-III levers* always produce *excursion* gains. Class-I levers can produce either of the two. The principles of levers are essential to the understanding of the *biomechanics* of the musculoskeletal system (Chapter 18).



Fig. 1.6 The physics of a lever (explanation in text).

Work and energy

Work is done when the point of application of a force (F) moves through a certain distance (D). Stated mathematically,

Work done (W) =
$$F \times D$$

The SI unit of work is the *Joule*. One joule of work is done when a force of 1 N moves a body through 1 m.

Energy is the capacity for doing work and the unit of energy is the same as that of work, that is, *Joule*. The energy associated with motion is called *kinetic energy (KE)* and is given by the formula:

$$KE = \frac{1}{2}mv^2$$

where *m* is the mass of the body and *v* is its velocity. The amount of kinetic energy that a body can gain by falling under the effect of gravity gives a measure of its *potential energy (PE)* and is given by the formula:

PE = mgh

where m is the mass of the body, g is acceleration due to gravity, and h is the height through which the body can fall.

When work is done *by a body* by expending its own energy, the work done is said to be *positive*. For example, a body that falls through a certain height expends its potential energy and therefore the work done *by the body* is positive. Conversely, a body that is lifted against gravity gains in potential energy. Therefore, work is done *on the body, and the work done* is *negative*.

When a fluid is compressed by application of pressure P, the fluid gains in energy, which is at least partly in the form of heat. The work done on the fluid is therefore negative and is given by:

Work done
$$(W) = -\int PdV$$

where dV is the small decrement in volume through which it has been compressed. Conversely, for expanding against an incumbent pressure, the fluid has to expend energy and therefore it loses energy. The work done *by* the fluid is therefore positive and is given by:

Work done (W) =
$$+\int PdV$$

These concepts help us understand why the work done by the lungs or the heart is given by the area enclosed in its pressure–volume loop.

In the case of the lungs, the work done on the lungs is negative during inspiration because the lungs themselves do not expend any energy; rather, they are made to inflate by the inspiratory muscles. During inspiration, the lungs gain in elastic recoil energy. This recoil energy stored in the lungs is expended during expiration as the lungs deflate. Therefore, *the work done by the lungs during expiration is positive*. The work done on and by the lungs during inspiration and expiration are shown graphically in **Fig. 1.7A**.

When the work done during both inspiration and expiration are added, there is *a net small amount of negative work done* that is represented by the area enclosed within the *pressure-volume loop* (called the *hysteresis loop*). The negative work signifies that at the end of one breathing cycle, work has been done *on* the lungs *by* the respiratory muscles which have expended their energy. The lungs have not spent energy of their own; rather, they have gained some energy. The *energy gained* is the heat energy that has been generated by the frictional (viscous) forces inside the lungs.

In the same way, the area inside the *ventricular pressure–volume loop* of the cardiac cycle gives the positive work done by the ventricle in overcoming viscous resistance of blood flow (**Fig. 1.7B**).

Buoyancy

When a body is immersed in a fluid, *the fluid displaced pushes the body up so that the body loses weight*. The loss in weight is called *buoyancy* and it



Fig. 1.7 [A] Work done on the lung during breathing. [B] Work done by the ventricle during a cardiac cycle.

is equal to the weight of the fluid displaced. Providing buoyancy to the brain is an important function of the *cerebrospinal fluid*.

Surface tension

Surface tension is a property of liquids due to which a liquid surface behaves like a stretched membrane. Because of surface tension, a drop of fluid minimizes its surface area. It therefore assumes a spherical shape because the surface to volume ratio is minimum for a sphere. The fact that a bubble does not collapse indicates that the air inside it provides a distending pressure that exactly balances the collapsing pressure of the fluid shell.

The **law of Laplace** states that tension (T) in the wall of a cylinder is equal to the product of the transmural pressure (P) and the radius (R). The formula has several variations (**Table 1.2**) depending on the geometry of the surface (spherical or cylindrical) and its composition (liquid drop, liquid bubble, or air bubble) (**Fig. 1.8**). Applications of Laplace law in physiology assume P = 2T/R as an approximation, which is the formula for a spherical air bubble in air.

The law of Laplace helps explain several important physiological phenomena. (1) It explains how the *thin-walled capillaries* are able to withstand an internal pressure as high as 25 mm Hg, which is the normal capillary hydrostatic pressure. This is possible because capillaries have a very small radius R.

Table 1.2	Formulas	defining	Laplace	law
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	Spherical	Cylindrical
Liquid drop in air	2T/R	T/R
Air bubble in liquid	4T/R	2T/R
Air bubble in air	2T/R	T/R



Fig. 1.8 The Laplace law is applicable to any of the above (see Table 1.2).

Even though the wall tension is low, the small value of R in the denominator makes a very high P possible. (2) The law of Laplace puts the dilated heart at a disadvantage. When the radius R increases, the wall tension T must go up proportionately if the ventricular pressure P is to be maintained. (3) In accordance with the Laplace law, the lower the functional residual capacity of the lungs, the more difficult it is to inflate it. (4) Because of Laplace law, the greater the gastric filling, the lower is the pressure that causes gastric emptying. This is obviously beneficial to the process of digestion. (5) Laplace law explains why a reduction in detrusor muscle tension prevents a rise of intravesical pressure even as the urinary bladder fills up to greater volume.

Viscosity

Viscosity is *fluid friction*. When fluid moves along a tube, it does so in the form of multiple layers or laminae that slip on one another, moving at different velocities due to friction between the layers. The lamina at the middle of the blood vessel moves fastest while the one closest to the vessel wall does not move at all. Thus, there is a velocity gradient of laminae, which is called the *shear rate*. A fluid has *1 poise* of viscosity if there is a frictional force of 1 dyne/cm² between its layers when flowing at a shear rate of 1 cm/s. A *Newtonian fluid* is one in which the *viscosity is independent of the shear rate*. Blood is not a Newtonian fluid.

Just as friction affects the velocity of a body, viscosity affects the velocity of fluid flow. In a long narrow tube of uniform radius, the relation of the flow rate (Q) with the pressure gradient ($P_A - P_B$), that is, the pressure difference at the two ends of the tube, fluid viscosity (η), tube radius (R), and tube length (L) is given by the *Poiseuille-Hagen formula*:

$$Q = (P_A - P_B) \times \frac{\pi}{8} \times \frac{1}{\eta} \times \frac{R^4}{L}$$

This law is important in the understanding of hemodynamics. Since resistance varies inversely with the fourth power of the radius, even *small changes in the vessel diameter cause large variations in blood flow through it*, enabling effective regulation of blood flow through vascular beds. The physiological relevance of the Poiseuille-Hagen formula is best brought out by the differences in the blood flow in the renal cortex and the renal medulla (see p 377), where blood viscosity, capillary length, and capillary diameter all have a role.

At high velocities, the flow of fluid becomes turbulent and does not remain streamlined. The probability of turbulence is related to the diameter of the vessel and the viscosity of the blood. This probability is expressed by the *Reynolds number*:

$$Re = \frac{\rho DV}{\eta}$$

where Re is the Reynolds number, ρ is the density of the fluid, D is the diameter of the tube (in cm), V is the velocity of the flow (in cm/s), and η is the viscosity of the fluid (in poise). The higher the value of Re, the greater the probability of turbulence. When Re < 2,000, flow is usually not turbulent whereas if Re > 3,000, turbulence is almost always present. Turbulence of blood is responsible for *cardiac murmurs* and the *Korotkov sounds*.

The Poiseuille-Hagen formula can be rewritten as:

$$(P_A - P_B) = Q \times \frac{8}{\pi} \times \eta \times \frac{L}{R^4}$$

Thus when the flow rate, fluid viscosity, and tube radius remain constant, the pressure drop $(P_A - P_B)$ along a tube is directly proportional to the length of the tube and inversely proportional to the tube radius, as explained in **Fig. 1.9**.

Bernoulli principle

When a constant amount (Q) of fluid flows through a tube, the total fluid energy, that is, the sum of its *kinetic energy, pressure energy*, and *potential energy*, remains constant (**Fig. 1.9**). This is known as *Bernoulli principle* and it helps in understanding several important hemodynamic principles. It explains, for example, why the fluid pressure is low in a blood vessel at places where its radius is less² (**Fig. 1.9**). It also explains the suction effect of venous blood flow on the thoracic duct terminating in the vein (see **Fig. 39.7**).

Heat

Heat always flows from a higher temperature to a lower temperature. When the temperatures of two bodies are equal, no heat transfer occurs between them. (1) In *conduction*, transfer of heat occurs through a medium whose molecules cannot move about freely. Thus, when we hold an iron rod in fire, the iron atoms vibrate and transfer the heat from the fire to the hand through the rod. However, the



Fig. 1.9 A horizontal tube is fitted with uniformly spaced manometers for measuring the pressure drop. [A] The pressure falls uniformly with distance in accordance with the Poiseuille-Hagen formula. [B] The pressure falls in the constricted segment in accordance with Bernoulli principle. Beyond the constricted segment, the pressure rises again. The depiction is not entirely correct: the correct pressures are depicted immediately below. [C] The pressure in the constricted segment is low in accordance with Bernoulli principle and the pressure drop along the segment is steeper in accordance with the Poiseuille-Hagen formula. (D) The fluid rises higher in the last manometer because it captures a part of the fluid's kinetic energy and converts it into pressure energy in accordance with Bernoulli principle.

iron atoms do not move from their fixed places. (2) In *convection*, the molecules of the medium transfer heat by actually moving about, carrying the heat with them. *Evaporative cooling* is an example: The water molecules vaporize and move away, carrying the heat with them. The *caloric stimulation test* for testing vestibular functions is based on the convective currents set up inside the vestibular apparatus. (3) In *radiation*, no medium is required. It is through radiation that heat from the sun travels through space and reaches us.

²The fact that both Poiseuille-Hagen formula and Bernoulli principle give the effect of tube diameter on fluid pressure need not be cause for confusion. The two formulas deal with different aspects of fluid energy. The Poiseuille-Hagen formula deals with the conversion of fluid pressure into heat and the resultant loss of fluid pressure as the fluid flows through a long tube of uniform diameter. It does not deal with the other forms of fluid energy like kinetic energy or potential energy. On the other hand, Bernoulli principle deals with the interconversion of the three different forms of fluid energy and not with its conversion into heat energy.

Heat transfer occurs through all possible modes. If a medium is present and the molecules are free to move about, heat will travel through convection. If the molecules cannot move about, heat will travel through conduction. Regardless of whether a medium is present or not, some heat will always travel through radiation.

A knowledge of the modes of heat transfer is important to the understanding of thermoregulation in the body and explains our behavioral responses to changes in environmental temperature. For example, it is through convection that the circulating blood maintains a fairly uniform temperature throughout the body. The body is cooled through the *evaporation* of sweat (convection). We seek shade because it cuts off the radiation heat from the sun although we still feel the convective heat of hot air or the conductive heat of the ground we lie upon. We wear dark, coarse-textured clothes in winter because dark surfaces absorb radiated heat. We wear light-colored clothes in summer because they light surfaces reflect back heat radia*tion*. Thick woolen clothes that trap air in them reduce conductive and convective losses of body heat in winter.

Light

Light bends as it passes from air into a denser medium or when it emerges out of the medium into air. This bending is known as refraction and the extent to which it bends while passing in and out of the medium is given by the *refractive index* (μ) of the medium. The refractive index of water is 1.33. The refractive indices of the various compartments of the eye are shown in **Fig. 114.1**.

Refraction of light underlies the formation of an image by the lens. A knowledge of how lenses work helps in understanding the refraction in the eye. The basic formula for lenses is:

$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

where u is the distance of the object from the lens, v is the distance of the image from the lens, and f is the focal length of the lens. The distances u, v, and f may be positive or negative, depending on whether the measurements are made along the direction of the light or against it (**Fig. 1.10**). The focus is the point where parallel rays passing through the lens would converge (in the case of a convex lens) or appear to diverge (in the case of a concave lens). The focal length of a concave lens is positive while the focal length of a concave lens is negative.



Fig. 1.10 Ray diagrams showing the focal point of a convex lens (*above*) and a concave lens (*below*). In the examples illustrated here, the focal length of the convex lens is +6 cm and the focal length of the concave lens is -6 cm.

The **power of a lens** is expressed in *diopter (D)* and is the *reciprocal of its focal length in meters*. Thus the power of a convex lens with focal length of +25 cm is +4 diopter, whereas the power of a concave lens of -50 cm is -2 diopter. The power of the intraocular lens can be increased by contracting some of the intraocular muscles. This phenomenon is called *accommodation*. When two coaxial lenses are placed together, their *diopteric powers are added algebraically*. This forms the basis of *correction of refractory errors by using external lenses*.

The physics of image formation is best understood by integrating it with the physiology of sensory perception, because whatever we see around us is essentially the sensory projection of images formed on our retina. Consider a point object (O) and its point image I formed by a convex lens L (**Fig. 1.11**). A point image is formed when all the rays diverging from a point object are made to converge at a single point using a convex lens. In Fig. **1.11A**, the image I_r (r for real) is formed in front of the eye. After converging at I, the rays diverge again and therefore the point image (the point of convergence of rays) behaves like a point object (the point of divergence of rays). Hence the image is called a *real image.* The diverging rays from I_r converge on the retina after passing through the convex lens of the eye. Past sensory experience of the observer's brain tells it that the rays forming the retinal image are originating from point I, and, therefore, the brain "sees" an image at point I. This "calculated guess" made by the brain is known as *sensory projection*. In making the projection, the brain takes into consideration, among other factors, the extent of accommodation required by the intraocular muscles.

In **Fig. 1.11B**, the convex lens L bends the divergent rays from the object but not enough to



Fig. 1.11 The optics of image formation of point objects.

make them converge in front of the eye. It is the intraocular lens that finally converges the rays on to a point on the retina. As in the previous case, the brain projects the retinal image to the point where the divergent rays incident on the eye seem to be originating from. Hence, the brain "sees" an image at point I_v. Unlike I_r, no rays are actually diverging from I_v; they only appear to do so due to sensory projection. Hence, I_v is called a *virtual image* (virtual = amounting to). Stated simply, an image is real if it is formed by the convergence of rays. *The image is virtual if it is visible at a site where there is no convergence of rays.* Going by this definition, the image formed on the retina of the eye is a real image.

The images formed when the object is located at different distances from the lens are shown in **Fig. 1.12**. These ray diagrams can be easily



Fig. 1.12 The optics of image formation of objects placed greater than two focal lengths away (*above*), at twice the focal length (*middle*), and at focal length (*below*).

constructed by remembering that (1) rays parallel to the principal axis converge at the focus after passing through the lens and (2) the rays passing through the optical center (3) of the lens do not deviate.

How big does an object appear to the observer? The answer is that the nearer an object is to the eve, the bigger is the retinal image and the bigger it appears to the observer. However, how close we can bring an object to our eyes is limited by the power of our accommodation. Short-sighted people (myopes) see bigger images because they can bring the object nearer to the eye and still see it clearly. Another question arises here. Given two objects of different sizes placed at different distances from the eye, which one will appear bigger? The answer lies in the visual angle subtended by the two objects: The object that subtends a greater visual angle looks bigger (Fig. 1.13). The visual angle forms the basis of the testing of *visual acuity*. The visual angle subtended by an object is given by the formula:

Visual angle =
$$\tan^{-1} \frac{\text{Height of the object}}{\text{Distance of the object from the eye}}$$

Thus, if an 8.75 cm high object³ is kept at a distance of 60 m (i.e., 6,000 cm), the visual angle subtended by it will be:

- $= \tan^{-1} [8.75/6,000]$
- $= \tan^{-1} [0.00145]$
- = 0.0835 degree
- = 0.0835 × 60 minutes
- = 5.01 minutes

The retina is normally situated at the focus of the intraocular lens (see Fig. 114.4) and therefore when there is no accommodation, only objects at *infinity are clearly visible*, for example, the stars in a night sky. Anything nearer appears hazy. This can be verified by putting atropine (a cycloplegic) on the eye, which abolishes the power of accommodation. For the same reason, we see the maximally magnified images without straining our eyes when the object is kept at the focus of a magnifying glass and its virtual image is formed at infinity.⁴ Due to sensory projection, parallel rays falling on the eye result in a virtual image that is infinitely large and is formed at infinity. How big does an infinitely large image located at infinity appear to the eye? As already explained, the answer depends on the visual angle subtended at the eye by the virtual image.

³In the Snellen chart, the topmost letter is 8.75 cm high, which is readable by a normal person from a distance of 60 m (see Fig. 114.12).

⁴This point is stressed here because several textbooks of high school physics mention that when an object is kept at the focus of a convex lens, the rays become parallel and therefore no image is formed. That is incorrect.



Fig. 1.13 The visual angle increases as the object is brought nearer to the eye. Note that the greater the visual angle, the larger is the retinal image. When the object comes nearer than the near point, the retinal image becomes blurred.

Because the eyes do not have to be strained (accommodated) for seeing a virtual image at infinity, all optical instruments, including microscopes, are so designed that the *image formed is virtual and is situated at infinity*. A commonly observed virtual image at infinity is the *red eye* well known to photographers: The pupil appears red in a photograph that has been shot in dim light using flashlight (**Fig. 1.14**). Because the pupils are dilated in dim light, the *red choroid layer* beneath the retina is illuminated by the flashlight and gets photographed. The illuminated choroid, which is situated at the focus of the intraocular lens, sends out



Fig. 1.14 Red eye (Bruckner) reflex in a photograph shot in the dark using flashlight. The principle of direct oph-thalmoscopy is similar.

parallel rays from the pupil. These parallel rays are captured by the camera even from a distance of several meters. Image formation when the object is at focus is also of importance in understanding direct ophthalmoscopy and retinoscopy.

Fig. 1.12 also shows that the nearer an object is to the focal point F, the greater the distance between the image and the lens. In the eye, the distance between the lens and the retina is fixed at 17 mm and the maximum power of the lens that can be attained after full accommodation is 69 diopters which is equivalent to a focal length of 14.5 mm. Substituting these values in the lens formula, we get u = 10 mm, which is as close the object can get to our eyes without blurring the retinal image and is called the *near point*.

Waves and sound

A wave propagates through a medium when the particles of the medium oscillate rhythmically about their mean position. The wave is called *transverse or longitudinal* depending on whether the plane of oscillation of the particles is perpendicular or parallel to the direction of wave motion. A *transverse wave* has alternate crests and troughs (**Fig. 1.15**). The ocean waves or the ripples in a pool of water or the fluttering of a flag in the wind are examples of transverse waves. Transverse waves



Fig. 1.15 Characteristics of wave motion. [A] Transverse and longitudinal waves. [B] Waves with different frequency and amplitude. [C] Waves with a phase difference. [D] Wave summation. Note that the wave in red color is formed by the summation of the two waves shown in blue, one of which has a lower frequency (fundamental wave) and the other has double the frequency (harmonic wave). The shape of the summated wave is different from the component waves, and gives the wave a characteristic sound quality or timbre.

are also set up on the basilar membrane of the cochlea (see **Fig. 118.6**). A *longitudinal wave* has alternate zones of condensation and rarefaction. Sound waves in air are longitudinal waves.

The *frequency of a wave* is the number of waves produced in 1 second and is expressed in *Hertz* (Hz). It is inversely related to its wavelength. Two waves with the same frequency can have a *phase difference* or *phase lag* (**Fig. 1.15C**). For example, if at any point of time, one wave is at its crest (i.e., at 90 degrees) and the other is at its trough (i.e., at 270 degrees), the two waves are 180 degrees out of phase. The term *phase difference* or *phase lag* has been used in this book in the context of fluctuations in blood gases in Cheyne–Stokes breathing and in the ionic basis of cardiac pacemaker potentials. Two waves with different frequencies and amplitudes can summate to produce a *complex wave*. Such complex waves form the basis of the quality or timbre of sound waves (**Fig. 1.15D**). The characteristics of a sound wave, namely, its pitch, loudness, and timbre, are discussed below.

Pitch The pitch (or tone) of the sound is what is perceived by the human ear as higher or lower musical notes: It is directly related to its frequency. The greater the frequency, the higher is the tone. *Pitch discrimination* by the human ear is best in the range of 1,000 to 3,000 Hz.

Intensity and loudness A sound wave is essentially a traveling pressure wave and therefore the amplitude of a sound wave is expressed as the maximum pressure variation in it. The *intensity* of a sound wave is the amount of energy (in joule) transported by the sound wave in unit time (1 s) per unit area (1 m²), across a surface perpendicular to the direction of propagation. The intensity of a sound wave is directly proportional to the square of its pressure amplitude. The pressure amplitude of the faintest sound that can be heard is about 3×10^{-5} Pa and the corresponding intensity is 10^{-12} J/s/m². A more convenient unit for expressing sound intensity is the *decibel (dB)*.

Number of dB = 10 log $\frac{\text{Intensity of the sound}}{\text{Intensity of barely audible sound}}$

The term *loudness* refers to the listener's subjective perception of the magnitude of a sound sensation. Loudness increases with intensity, and the relation between the two is empirical, which is given by the *Weber–Fechner law* or any of its modifications (see **Fig. 103.17**).

Since the decibel scale is a logarithmic scale, every 10 dB represents a 10-fold increase in sound intensity. The *threshold of hearing* (i.e., the intensity of the faintest audible sound) is *zero decibel*. A sound is 10 times louder than threshold at 10 dB, 100 times louder at 20 dB, a million times louder at 60 dB, and 10 billion times louder at 100 dB. The usual loudness of speech is 65 dB. A 100 dB sound damages the peripheral auditory apparatus while 120 dB causes pain, and 150 dB causes permanent damage to the hearing apparatus.

Timbre or quality Most musical sounds are made of complex waves formed by the summation of a high-amplitude wave (fundamental frequency) with several other waves of smaller amplitudes whose frequencies are multiples of the fundamental frequency (harmonics or overtones). The *fundamental frequency* determines the pitch of the sound while the *overtones* give the sound its characteristic timbre or quality. Variations in timbre enable us to distinguish tones of the same pitch produced by different musical instruments.

A mathematical theorem called the Fourier transform makes it possible to express any wave with a given frequency and amplitude as the sum of a fundamental frequency and its numerous harmonics. Fourier transform has tremendous application in engineering. A well-known example is the musical synthesizer in which the tone of any musical instrument can be synthesized by mixing several multiples of a fundamental frequency in appropriate proportions of their amplitudes. Fourier transform has been applied to biological signals too, for example, for data reduction in electroencephalogram. Finally, it is interesting to note that the basilar membrane of the cochlea works out the Fourier transform of the sound waves: The sound wave breaks up into its component frequencies on the basilar membrane and each component registers its maximum amplitude at a different site of the basilar membrane. This information is conveyed separately to the brain which is then able to "synthesize" the quality of the sound.

Electricity

Electrical charge Atoms are made of protons, neutrons, and electrons. A proton has a unit positive charge, an electron has a unit negative charge, and neutrons do not have any charge on them. A body containing equal numbers of protons and electrons is electrostatically neutral. When the number of electrons in a body exceeds the number of protons in it, the body develops a *negative charge*. Conversely, it develops a *positive charge* when the number of electrons in it. The SI unit of charge is the *Coulomb* which equals the charge of 6.242×10^{18} electrons.

Current The *flow of charged particles* is called an electric current. The SI unit of current is the *Ampere*. A flow of 1 C of charge every second is 1 A current. Electricity is the flow of negatively charged electrons from a negative to positive potential. Conventionally, however, electricity is assumed to be the flow of positively charged particles from a positive to negative potential.

Potential The potential of a body is the work done when a charge of +1 C approaches the body from infinity under the effect of its attractive or repulsive force. If the work done is 1 J, the potential of the body is said to be 1 V, which is the SI unit of potential. Two charged bodies have **1** V potential *difference* if 1 J of work is done in moving a charge of +1 C from one body to the other.

Resistance The resistance of a conductor determines how much current it allows to pass through it when a potential difference is applied across it: for a given potential difference across a conductor, the current flowing through the conductor is inversely proportional to its resistance. This is known as the *Ohm law*. If the current is 1 A when the potential difference is 1 V, the resistance is said to be 1 Ω , which is *the SI unit of resistance*. Conductance is the reciprocal of resistance and its SI unit is Mho.

Voltage = Current × Resistance

An important derivation of Ohm law is that when resistances (R1, R2, R3...) are *connected in series* (**Fig. 1.16A**), the total resistance (R) is given by:

$$R = R1 + R2 + R3 \dots$$

When R1, R2, and R3 are *connected in parallel* (**Fig. 1.16B**), the total resistance is given by the formula:

$$1/R = 1/R1 + 1/R2 + 1/R3 \dots$$

The resistance of a conductor varies directly with its *length* and inversely with its *cross-sec-tional area*. This principle is important in the understanding of nerve conduction and explains why *nerve conduction velocity increases with axon diameter*.

Capacitance The potential of a body is directly proportional to the amount of charge it contains. The greater the amount of charge a body contains,



Fig. 1.16 Resistances in series [A] and parallel [B].

Box 1.1 What is Zero Potential?

Although earth is a stable reference for all electric potentials, it is impractical to express all potentials with reference to ground potential. Consider Fig. 55.2 showing the Warila pass. Its altitude is shown as 17,300 feet. The reference point here is the sea level. A more stable reference would be the center of the earth but that is unnecessary and inconvenient. Similarly, it is more convenient to measure the heights of the local peaks in reference to the average altitude of the surrounding terrain. Thus, all bioelectric potentials are expressed in reference to the potential of adjacent areas of the body, or to the average potential of the body.

the greater is its potential. However, the extent to which the potential rises when a given amount of charge is imparted to it will differ for different bodies. A body that can hold a large amount of charge without much rise in its potential is said to have a high capacitance. Stated mathematically,

$Capacitance = \frac{Charge}{Potential}$

Larger bodies have higher capacitance and, therefore, the *earth has almost an infinite capacitance*. Thus the potential of earth (ground potential) remains unchanged no matter how much charge enters it. This stable *ground potential* is assumed to be zero and serves as a *convenient reference for all electrical measurements* (Box 1.1). For the same reason, any charged body, when grounded, loses all its charge to the earth and its potential becomes zero.

A device that can store a large amount of charge is called a capacitor. A capacitor can hold a lot of charge and yet its potential remains low. On the other hand, a body with a low capacitance develops a high potential when it is charged. At high potentials, charge tends to "leak out" and hence a body with low capacitance cannot hold much charge. A capacitor can be built by sandwiching a thin sheet of dielectric (nonconducting material) between two parallel metal plates. Such a capacitor is called a **parallel plate capacitor**. When a potential difference is applied to the plates, a large amount of charge is stored in the plates.

The *nerve membrane behaves like a dielectric*, and when both its surfaces are layered with ions of opposite charges, it acts like a parallel plate capacitor (see **Fig. 10.1**). *Membrane capacitance* is an important determinant of membrane excitability and conduction velocity of nerve membranes.

Electricity and fluid dynamics

The concepts of electricity are relevant to fluid dynamics too and help in understanding several important hemodynamic phenomena. Conversely, simple analogies of fluid mechanics help in understanding certain electrical phenomena like capacitance. These analogies are explained below.

Fluid pressure is analogous to *electric potential* and fluid usually flows from high pressure to low pressure just as electric current flows from high to low potential. The amount of fluid flowing in unit time is analogous to *electric current*. Fluid resistance is quite similar to *electrical resistance*. The relationship between resistance, pressure drop, and flow rate in the blood vessels is similar to the relationship between the resistance, potential difference, and current:

Resistance = Pressure drop/flow rate

A similar formula is employed for defining blood flow resistance in vascular beds in terms of flow rate and perfusion pressure. Even the formulas for electrical resistances in series and parallel are valid for fluid dynamics and have important implications in hemodynamics. For example, most capillary beds are disposed in parallel to the heart while the portal beds are in series (Fig. 1.17). The physics of parallel circuits explains the phenomena of *circulatory "steal"* like coronary steal or subclavian steal: The electrical analogy is that when multiple resistors are connected in parallel, more current flows through resistors with lower resistance and vice versa. The electrical analogy also helps in understanding why the blood pressure falls when the resistance in any of the capillary beds decreases.

The *electrical capacitance* of a body can be compared with the fluid capacity of a container. A container with a large base is similar to a capacitor because it can store a large amount of fluid (analogous to charge) without its hydrostatic pressure (analogous to potential) increasing too much. On the other hand, the pressure in a narrow tube rises quickly when filled with fluid. For the same reason, *leakage of charge is higher when the capacity is low* (**Fig. 1.18A**).

Another similarity between electricity and fluid dynamics pertains to the measurement of potential. Consider two containers with fluid filled to different levels. For measuring their average potential, the two containers are connected to a graduated measuring tube as shown in **Fig. 1.18B**. The height of the fluid column in the graduated



Fig. 1.17 Circulatory beds in series and parallel with the heart. Note that the capillary beds that are in series constitute a portal system.



Fig. 1.18 Fluid analogy of electricity. [A] Fluid pressure and capacity are analogous to electric potential and capacitance. Shown here are two containers containing the same volume of fluid and with both having a small hole near their base. The container on the left has a broader base and therefore the hydrostatic pressure is low and leakage is much less. The container on the right has a narrow base. Hence the hydrostatic pressure is high and leakage is more. [B] A graduated tube interconnects two fluid-filled containers and is equidistant from both. The fluid pressure in the tube gives the mean of the fluid pressures in the two containers. However, the pressures in the two containers soon equalize unless the connecting limbs have high resistance to fluid flow.

tube gives the average fluid pressure in the two containers. The problem with this method is that since the two containers are interconnected, their pressures equalize very soon. The problem can be tackled by increasing the resistance of the connecting limbs. This analogy helps in understanding why it is important in electrocardiography to interconnect the three limb electrodes *only through a high (5,000 \Omega) resistor* for obtaining zero potential (see **Fig. 34.4**).

Electric field of dipoles

Electric field refers to the area of influence of an electric charge (or charges). The electric field of a single charged particle is depicted in **Fig. 1.19A**. Each vector in the diagram represents the direction and force with which a positive charge of 1 C moves (or tends to move) under the effect of the electric field. If an electric field is applied to a medium containing mobile charged particles, the charged particles start moving along the lines of the electric field, resulting in the flow of an electric current. This happens in body fluid where an electric field is set up by the heart.

A **dipole** is a pair of opposite charges lying close together. The electric field set up by a dipole is more complex. Each dipole results in the flow of current between the opposite charges along multiple pathways as shown in **Fig. 1.19B**. Although the conventional current flows from the positive to the negative charge, to a recording electrode placed at a distance, the current appears to flow along a vector directed from the negative to the positive charge.

Multiple dipoles located along a line result in a large resultant current. Each dipole generates a large field around it as shown in **Figs. 1.19C** and **1.19D**. Only currents that travel straight along the axis of the dipole add up and become strong enough to be picked up by a distant recording electrode. A knowledge of dipoles and their fields is essential to the understanding of *electrocardiography and electroencephalography*.



Fig. 1.19 [A] The electric field of a positive charge (pink) and a negative charge (blue). Each line represents the direction of the repulsive or attractive force exerted on a charge of +1 C. [B] The lines of force around a dipole. [C] The lines of force when two dipoles are placed side by side. [D] When several dipoles are lined up, the current flowing along the long axis of the dipoles summate and is recordable by a distant electrode.

REVISION QUESTIONS

- 1. Gravity affects the blood pressure when the subject is standing but not when he is supine. Why?
- 2. When the vertices of the Einthoven triangle is connected together, the nodal point is at zero potential. Which branch of mathematics explains it?
- 3. What is the difference between gravitational force and g-force? What are Gx, Gy and Gz? What is zero Gz and when is it experienced?
- 4. In a sphygmomanometer, the 1 cm calibration is actually a little less than 1 cm. Why?

- 5. The total work done on the lung during the breathing cycle is said to be negative. Why?
- 6. The lower the functional residual capacity of the lungs, the more difficult it is to inflate it. This observation is in accordance with which law of physics?
- 7. Is blood a Newtonian fluid? Give reasons.
- 8. Even small changes in vessel diameter cause large variations in blood flow through it. This observation is in accordance with which law of physics?
- 9. What are the factors that (1) affect the flow rate of a fluid, and (2) tend to make the flow of a fluid turbulent?
- 10. Circulation of blood maintains a fairly uniform temperature throughout the body? Which mode of heat transfer is at work in this case?
- 11. During near-vision, short-sighted people (myopes) see things bigger and better. Give reasons.
- 12. If the eye is photographed in dim light using flashlight, the pupil appears red. Why?
- 13. If the distance between the intraocular lens and retina is 17 mm and the power of the intraocular lens after maximum accommodation is 50 diopter, what will be the near point of the eye?

- 14. Which physical characteristic of sound determines its (1) pitch, (2) intensity or loudness, and (3) quality or timbre?
- 15. The basilar membrane of the cochlea performs a Fourier transform on the sound waves. What is Fourier transform?
- 16. How does the diameter of a conductor affect its resistance?
- 17. What is zero potential?
- 18. What is the product of fluid resistance and the flow rate of the fluid?
- 19. *True or false:* System capillary beds are disposed in parallel while portal capillary beds are disposed in series.
- 20. What is circulatory steal?
- 21. *True or false:* if two capacitors contain the same amount of charge, the one with lower capacity will have lower potential. Give reasons.
- 22. In electrocardiography, the zero potential for reference is obtained by interconnecting the three limb electrodes through a high resistor. Why is a high resistor used?